

The Nonhydrostatic Unified Model of the Atmosphere (NUMA): CG Dynamical Core

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http://faculty.nps.edu/projects/NUMA

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Overview of Existing Global Models

Model	Organization	Spatial Discretization	Grid Type	Time- Integrator
Unified Model (NH)	UK Met Office	Finite Difference (2 nd order)	Structured (lat-lon)	Semi-Implicit/ Semi- Lagrangian
FIM (Hydrostatic)	ESRL NOAA	Finite Volume (2 nd order)	Icosahedral	Explicit
MPAS (NH)	NCAR	Finite Difference (2 nd order	Unstructured (hexagons only)	Split-Explicit
NUMA (NH)	NPS/NRL	Spectral Elements/ Disc. Galerkin (arbitrary order)	Unstructured (any grid)	Semi-Implicit: 3D and 1D Vertical

Design Philosophy (2)

Unified Dynamics

- All limited-area models are nonhydrostatic.
 Resolutions of global models are approaching the nonhydrostatic limit (~10 km).
- Both limited-area and global models utilize the same equations.
- Engineer a common dynamical core for both models, then change grids, force, and boundary conditions.

Unified Numerics

- CG is more efficient for smooth problems at low processor counts.
- DG is more accurate for problems with sharp gradients and more efficient at high processor counts.
- Both EBGs utilize a common mathematical arsenal.
- NUMA allows the user to choose either CG or DG for the problem at hand.

Unified Code

- Code is *modular*, with a common set of data structures.
- New timeintegrators, grids, basis functions, physics, etc. may be swapped in and out with ease.
- Code is portable:
 Successfully
 installed on Apple,
 Sun, Linux, and
 IBM.

Non-Conservative Form (2NC)

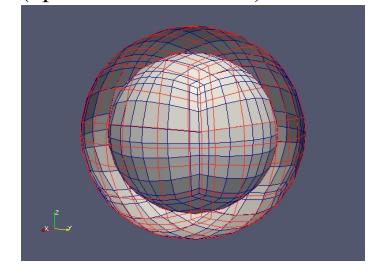
- •Consider the compressible Euler in Cartesian coordinates (not spherical).
- •Mass is conserved and energy can be conserved (up to time-truncation)

$$\frac{\partial \rho}{\partial t} + \nabla \bullet (\rho \mathbf{u}) = 0$$

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \bullet \nabla \mathbf{u} + \frac{1}{\rho} \nabla P + g \hat{\mathbf{k}} + \mathbf{f} \times \mathbf{u} = 0$$

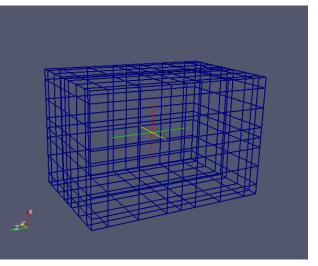
$$\frac{\partial \theta}{\partial t} + \mathbf{u} \bullet \nabla \theta = 0$$

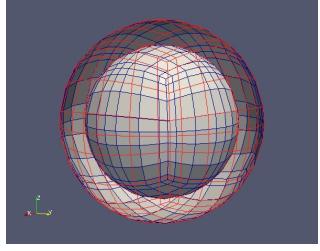
$$P = P_A \left(\frac{\rho R \theta}{P_A}\right)^{\gamma}$$

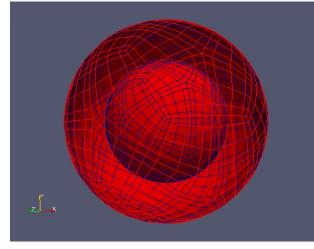


•The same model may be used for: global, limited-area, and urban-scale modeling (requires different grids, initial conditions, boundary conditions, and physics).

Example of 3D Grids







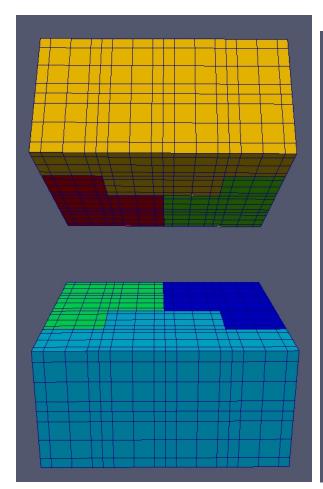
Mesoscale Modeling Mode

Global Modeling Mode (Cubed-Sphere)

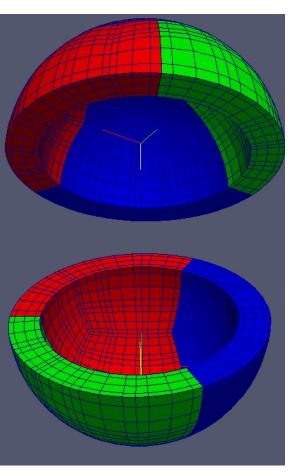
Global Modeling Mode (Icosahedral)

- NUMA runs in either Mesoscale (Limited-Area) or Global Mode.
- Currently, any (hexahedra-based) grid can be used including completely unstructured grids.
- Parallel Domain Decomposition handled by METIS.

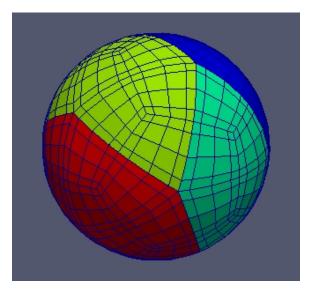
Domain Decomposition via METIS



1: Decomposition of a 3D Cartesian domain using 64 spectral elements (fourth order).

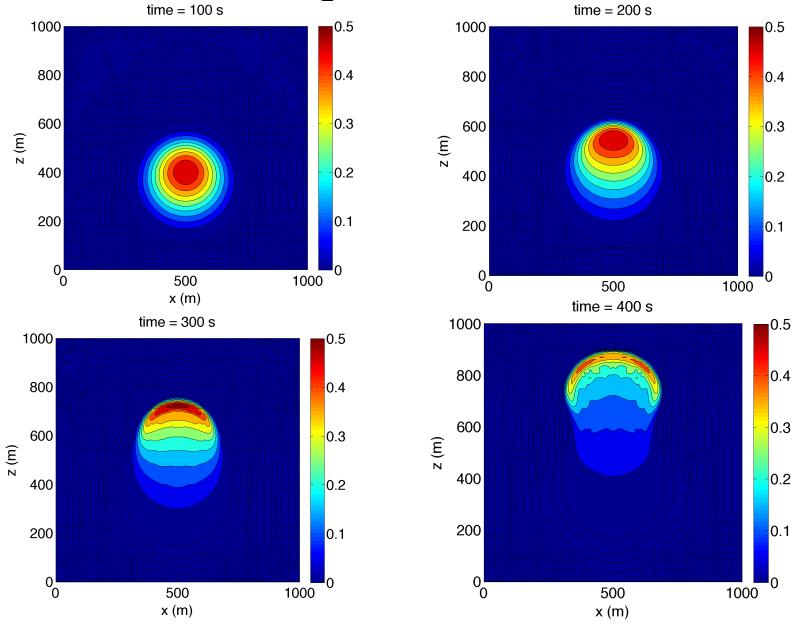


2: Decomposition of a "cubed sphere" using 96 spectral elements (fourth order).



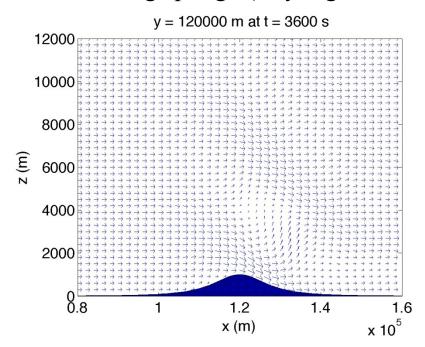
3: Decomposition of an "icosahedral sphere" using 96 elements (fourth order).

Rising Thermal Bubble: 3D

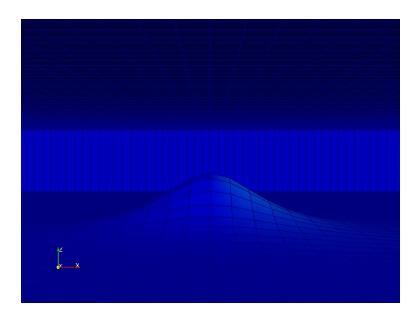


Orographic Flows: Linear Hydrostatic and Nonhydrostatic Mountain (3D) •Flow of U=20 m/s in an isothermal atmosphere.

- •LH Mountain: Solid of revolution of Witch of Agnesi:Mountain height = 1 m with radius 10 km.
- •Radiating boundary condition implemented on lateral and top boundaries using an absorbing sponge (Rayleigh friction).

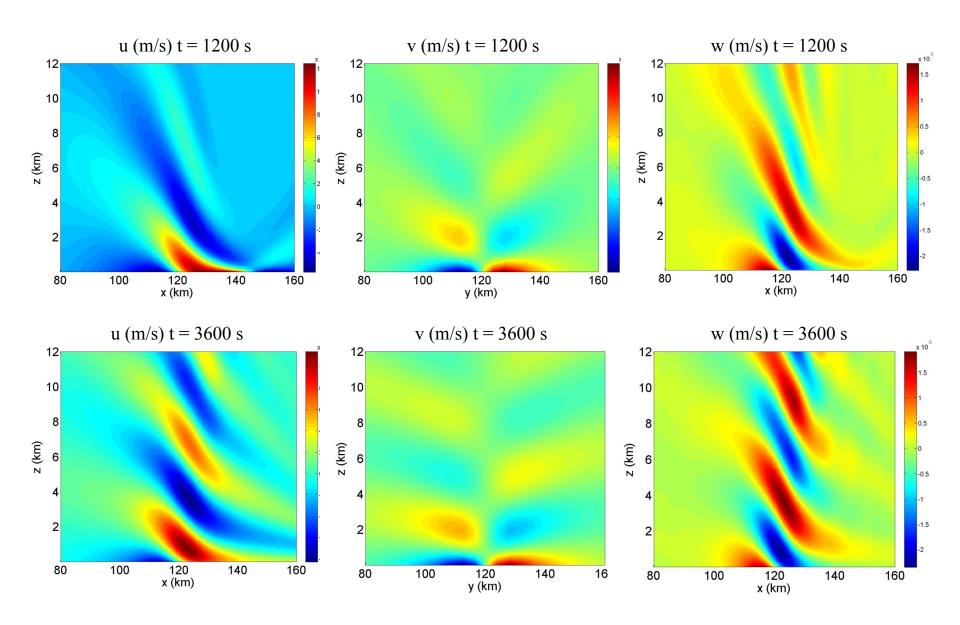


Non-Hydrostatic Mountain

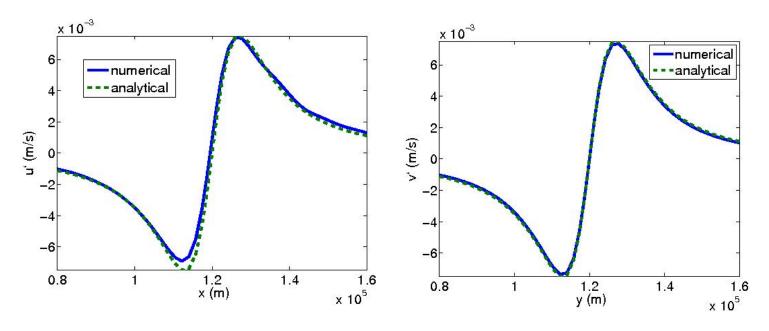


LH Mountain

Linear Hydrostatic Mountain (3D)



3D Linear Hydrostatic Mountain (Verification)



- Mountain case tests orography and sponge BC.
- Analytical approximations for flow over a LHM available in Smith (1980) on mountain surface.
- Decent agreement between theory and numerical model for downstream and cross-stream velocity perturbations.

Results (Global): Pressure Wave

- Proposed by Tomita and Satoh (2004) to test nonhydrostatic global atmospheric models.
- A pressure perturbation is applied to a hydrostatic, isothermal atmosphere

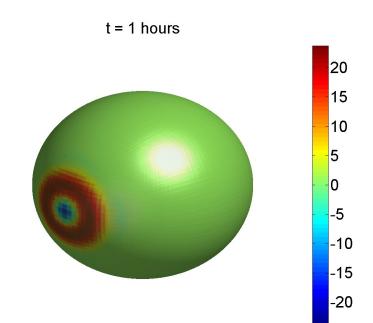
- •Top Level z_T =10 km
- •Cubed Sphere Grid with 6 x 12 x 12 x 6 = 5184 elements using 4^{th} order polynomials (~210 km horz. Resolution and 0.5 km vertical resolution)
- •Model run using Semi-Implicit TI w/ 5 s timestep

$$p' = \Delta p f(\lambda, \phi) g(z)$$

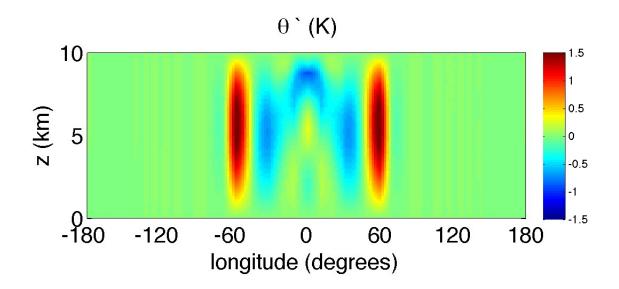
$$f(\lambda, \phi) = \frac{1}{2} H(R - r) \left[1 + \cos\left(\frac{\pi r}{R}\right) \right]$$

$$r = a \cos^{-1}\left(\cos\phi\cos\lambda\right)$$

$$g(z) = \sin\left(\frac{\pi z}{z_T}\right)$$

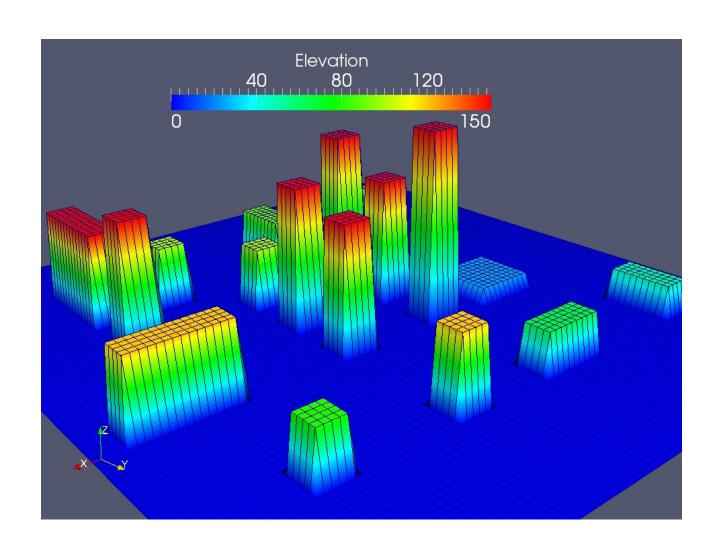


Results (Global): Inertia-Gravity Wave

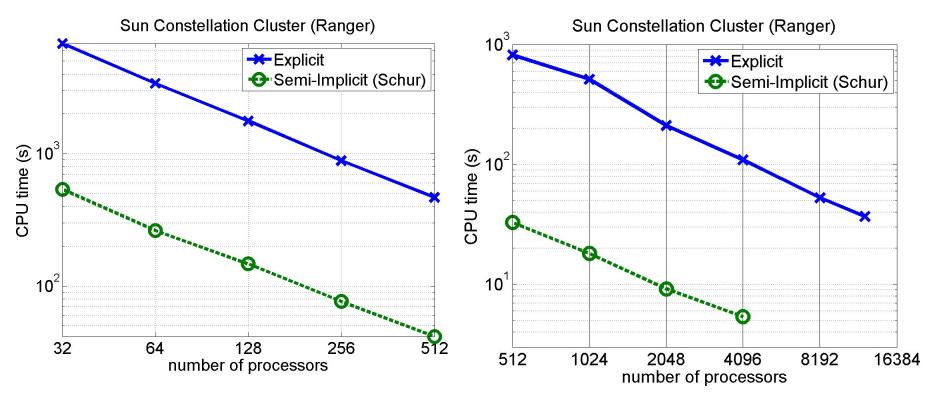


Potential Temperature after 48 hours with (240x0.5) km resolution

Urban-Scale Modeling



CG: Scalability (Explicit + Semi-Implicit)



Moderate Processor Counts: 110592 elements

Large Processor Counts: 262144 elements

Time-Steps

Explicit RK35: $\Delta t = 0.001 \text{ s}$

SI BDF2: $\Delta t = 0.01 \text{ s}$

Summary and Outlook

- NUMA Dynamical Core is quite mature:
 - 3D and MPI.
 - Can use either CG or DG methods.
- We will continue testing the dry dynamics and improve the model to make it as user-friendly as possible.
- Future Projects:
 - We are implementing sub-grid scale parameterizations to NUMA
 - Need more resources added to implement sub-grid scale parameterization, data assimilation, testing, etc.

Backup Slides

Conservative Form (2C)

- •Mass is conserved but not energy.
- •Conservation (or flux) form is required by DG machinery.

$$\frac{\partial \rho}{\partial t} + \nabla \bullet \mathbf{U} = 0$$

$$\frac{\partial \mathbf{U}}{\partial t} + \nabla \bullet \left(\frac{\mathbf{U} \otimes \mathbf{U}}{\rho} + P\mathbf{I}\right) + \rho g \hat{\mathbf{k}} + \mathbf{f} \times \mathbf{U} = 0$$

$$\frac{\partial \Theta}{\partial t} + \nabla \bullet \left(\frac{\Theta \mathbf{U}}{\rho}\right) = 0$$

$$P = P_A \left(\frac{R\Theta}{P_A}\right)^{\gamma}$$

$$\mathbf{U} = \rho \mathbf{u}$$

$$\Theta = \rho \theta$$

2D Inertia-Gravity Wave

100,000

Х

200,000

300,000

- •Standard test suite for 2D mesoscale problems (Skamarock, Doyle, et. al.)
- •Potential temperature perturbation after 3000 s for 250 m resolution (120 by 1 by 4 elements) and 10-th order polynomials.

•2D and 3D results agree to 8 decimal places. 8000 6000 θ, (Κ z (m) 4000 2000 0.5 2.5 1.5 x (m) x (m) x 10⁵ x 10⁵ SE1 DG2 10000 7500 5000

300,000

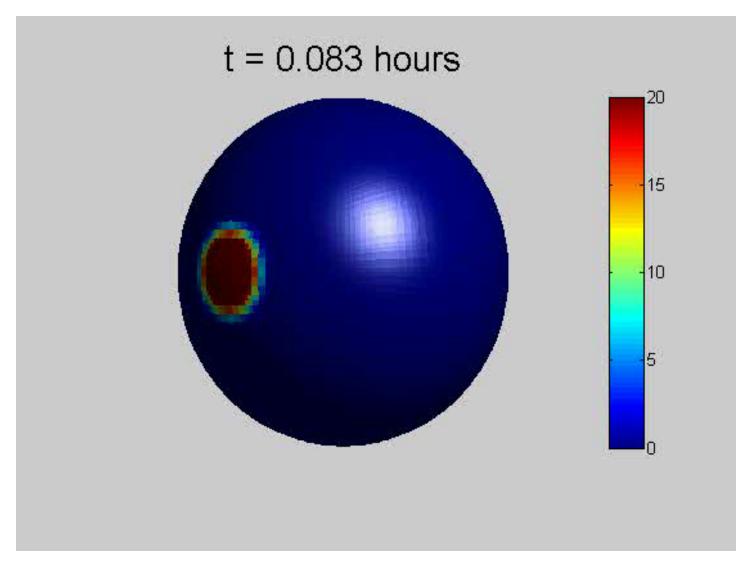
200,000

2500

CG-NUMA run with 1 element in y-direction.

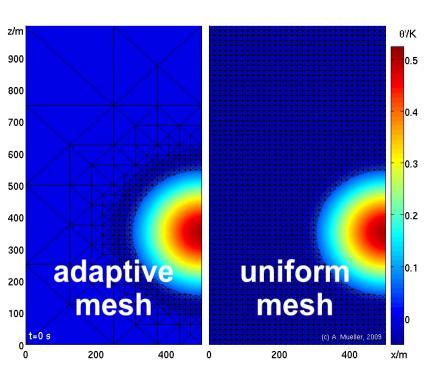
2D Density Current results for Giraldo and Restelli (2008).

Results (Global): Pressure Wave



- •Acoustic (perturbation) field shown at central vertical level (5 km).
- •Wave returns to initial state after about 32 hours, yielding a speed of sound of 348 m/s.

Non-hydrostatic Adaptivity Examples (Müller, Behrens, Giraldo, Wirth 2010)

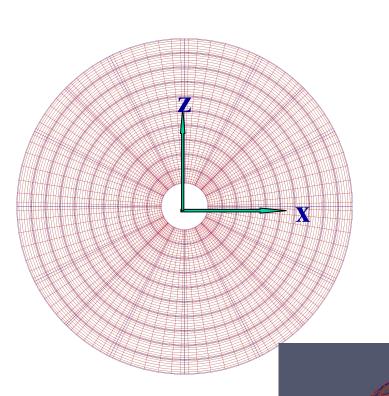


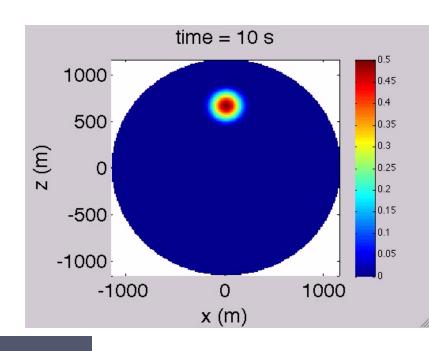
θ' / K 800 0.4 700 600 0.3 500 0.2 400 300 Warm air bubble 0.1 after 0 seconds. order of polynomials: 3 1000 x/m 800

Rising Thermal Bubbles

Two (Warm/Cold) Thermal Bubbles

Rising Thermal Bubble (Global)

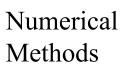




Overview of Existing Limited-Area Models

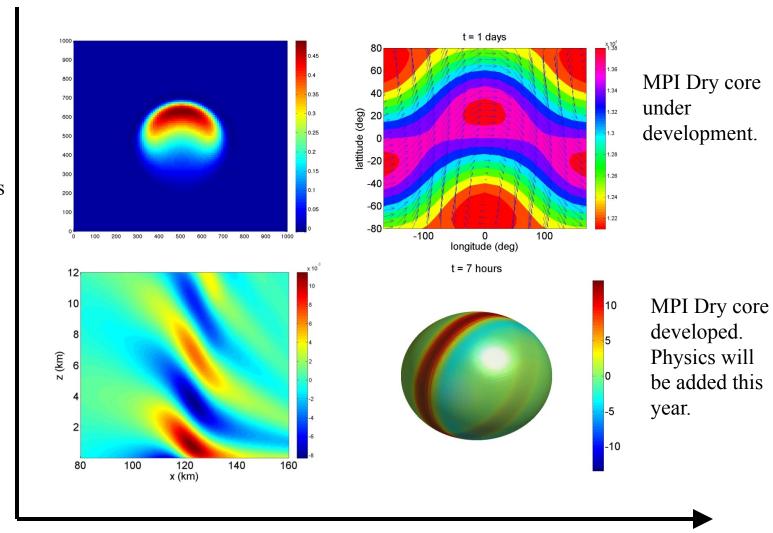
Model	Organization	Spatial Discretization	Grid Type	Time- Integrator
WRF	NCAR	Finite Difference	Structured	Split-Explicit
COAMPS	NRL-Monterey	Finite Difference	Structured	Split-Explicit
Lokal Modell	DWD	Finite Difference	Structured	Split-Explicit/ Semi-Implicit
NUMA	NPS/NRL	Spectral Elements/ Disc. Galerkin	Unstructured (any grid)	Semi-Implicit: 3D and 1D Vertical

Design Philosophy (1)



DG (Discontinuous Galerkin)

CG (Continuous Galerkin)

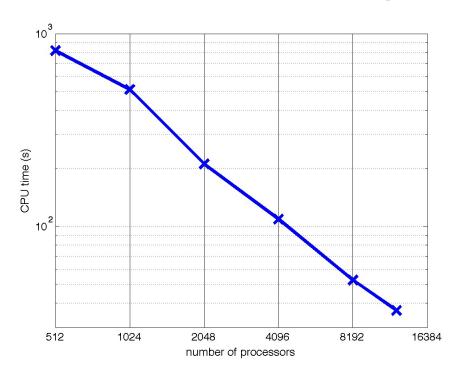


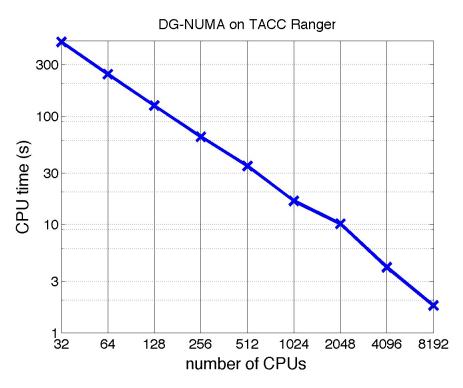
Limited-Area (Mesoscale)

Global

Scale

Performance of the NUMA Model (3D Rising Thermal Bubble)





Continuous Galerkin

Discontinuous Galerkin